



Queen Mary  
University of London

## BSc/MSci EXAMINATION

PHY-215 Quantum Physics

Time Allowed: 2 hours 15 minutes

Date: 22/05/08

Time: 10:00

Answer ALL questions in section A. Answer ONLY TWO questions from section B. Section A carries 40 marks, each question in section B carries 30 marks. An indicative marking-scheme is shown in square brackets [ ] after each part of a question.

COMPLETE ALL ROUGH WORKINGS IN THE ANSWER BOOK AND CROSS THROUGH ANY WORK WHICH IS NOT TO BE ASSESSED.

NUMERIC CALCULATORS ARE PERMITTED IN THIS EXAMINATION.

Speed of light	$c$	$3.0 \times 10^8 \text{ ms}^{-1}$
Planck's constant	$h$	$4.14 \times 10^{-21} \text{ MeV s}$ $= 6.63 \times 10^{-34} \text{ J s}$
	$\hbar$	$= 6.58 \times 10^{-22} \text{ MeV s}$
Electron/Positron Rest mass	$m_e$	$\approx 0.5 \text{ MeV}/c^2$
Proton Rest mass	$m_p$	$\approx 1 \text{ GeV}/c^2$
permittivity of free space	$\epsilon_0$	$8.85 \times 10^{-12} \text{ C}^2/(\text{Nm}^2)$
Electron Charge	$-e$	$= -1.6 \times 10^{-19} \text{ C}$
	1 eV	$= 1.6 \times 10^{-19} \text{ J}$
Boltzmann constant	$k_B$	$1.38 \times 10^{-23} \text{ JK}^{-1}$

Examiners: Dr. R. Russo and Prof. D. Dunstan

YOU ARE NOT PERMITTED TO START READING THIS QUESTION PAPER UNTIL INSTRUCTED TO DO SO BY AN INVIGILATOR

Questions:

Section A Answer all questions in this section.

- A1. State the Stefan-Boltzmann law for the total intensity of the electromagnetic radiation emitted by a blackbody. Is it possible to explain this law by means of classical physics only? Explain your answer. [5]
- A2. The total radiation emitted by a certain star is a factor 16 times that of a second star of equal size. Calculate the ratio between the temperatures of the two stars. [3]
- A3. Describe briefly Young's double slit experiment to demonstrate the phenomenon of interference between two monochromatic and coherent waves of the same frequency. [4]
- A4. The maximum wavelength of electromagnetic radiation that will result in the photoelectric emission of electrons from a sample of silver is  $2.6 \times 10^{-7}$  m. Find the work function for silver. [4]
- A5. Consider electrons of kinetic energy equal to 1 eV. Calculate the de Broglie wavelength,  $\lambda$ , of these electrons, justifying any approximation you may make. [5]
- A6. Use de Broglie's idea of standing waves to find a quantization condition on the angular momentum of a particle moving around a circular orbit. [3]
- A7. In Bohr's model for the hydrogen atom the electron energy levels are given by

$$E_n = -\frac{m_e e^4}{8\epsilon_0^2 h^2 n^2}, \quad \text{with } n = 1, 2, \dots$$

Derive the wavelength of the electromagnetic radiation that is capable of exciting the electron from the second ( $n = 2$ ) to the third ( $n = 3$ ) level. [5]

- A8. State the Heisenberg uncertainty principle and briefly comment on its meaning. [4]
- A9. Use Heisenberg uncertainty principle to estimate the minimal kinetic energy of a particle of mass  $m$  confined to a box of size  $L$ . [4]
- A10. Consider a harmonic oscillator of mass  $\mu = 1 \times 10^{-20}$  kg and Hooke's constant  $k = 1 \times 10^3$  kg/s<sup>2</sup>. What is the energy of the ground state according to Quantum Mechanics? [3]

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**Section B: Answer two questions in this section.**

**B1.** Consider an electron that is constrained to be in a one-dimensional box of size  $L$ , but is otherwise free to move inside the box.

(i) Write down the (time independent) Schrödinger equation for this particle, the boundary conditions for the wavefunction  $\Psi$  and find an expression for the energy levels. [12]

(ii) Consider the process where the electron decays from the  $n^{\text{th}}$  energy level to the ground state by emitting a photon. Find the wavelength of the emitted photon as function of  $L$ ,  $n$  and  $m_e$ . [8]

(iii) Consider now an electron that can freely move in a two dimensional square box. What are the energy levels in this case? Please motivate your answer. [10]

**B2.** (i) Describe the main features of the Compton-scattering between X-ray photons and free electrons initially at rest. [8]

(ii) By using energy and momentum conservation derive the following relation:

$$\lambda' - \lambda = \frac{h}{m_e c} (1 - \cos \theta),$$

where  $\lambda$  is the wavelength of the incident X-rays and  $\lambda'$  that of the outgoing ones and  $\theta$  is the angle between the incident and the outgoing X-rays. [14]

(iii) In a Compton experiment, the X-rays scattered through an angle  $\theta = 60^\circ$  have wavelength  $\lambda'$  which is 10% bigger than the wavelength  $\lambda$  of the incident X-rays. What is the energy of the incident X-rays? [8]

**B3.** In the Bohr model of the hydrogen atom angular momentum  $L = mvr$  is quantized to be  $n\hbar$  where  $n$  is a positive integer.

(i) Assume that the nucleus is at rest. By considering centripetal and electrostatic forces, find an expression for the radius of the  $n$ -th Bohr orbit. [10]

(ii) Find the speed of the electron in the  $n$ -th Bohr orbit, and hence show numerically why a non-relativistic treatment is justified. [10]

(iii) Consider an ionized Helium atom  $\text{He}^+$ , that is an ion with a nucleus of charge  $2|e|$  and a single electron. Use the same approach as in point (i) above to estimate the ionization energy required to remove the remaining electron. [10]

**B4.** (i) Let  $\Psi(x) = A(1 - x^2)$  be a wavefunction describing a particle that is confined to the region  $-1 \leq x \leq 1$ . Normalize this wavefunction appropriately and calculate the average position and momentum for this particle. [10]

(ii) Use the same wavefunction and calculate the probability of finding the particle in the region  $1/2 \leq x \leq 1$ . [8]

(iii) Use the same wavefunction and verify explicitly that the uncertainties for the position and momentum do satisfy the Heisenberg principle. [12]

End of Examination Paper  
Dr R. Russo